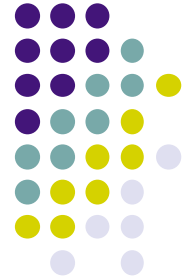


Calculations with environments



- The abstract machine does two kinds of calculations with environments
- **Adjunction:** $E_2 = E_1 + \{X \rightarrow y\}$
 - Add a pair (identifier \rightarrow variable) to an environment
 - Overrides the same identifier in E_1 (if it exists)
 - Needed for **local** $\langle x \rangle$ **in** $\langle s \rangle$ **end** (and others)
- **Restriction:** $E_C = E_{|\{X, Y, Z\}}$
 - Limit identifiers in an environment to a given set
 - Needed to calculate the contextual environment

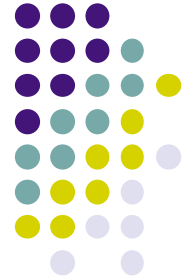


Adjunction

- For a **local** instruction

```
local X in (E1)  
  X=1  
  local X in (E2)  
    X=2  
    {Browse X}  
  end  
end
```

- $E_1 = \{\text{Browse} \rightarrow b, X \rightarrow x\}$
- $E_2 = E_1 + \{X \rightarrow y\} = \{\text{Browse} \rightarrow b, X \rightarrow y\}$



Restriction

- For a procedure declaration

local A B C AddB **in**

A=1 B=2 C=3 (**E**)

fun {AddB X} (**E_C**: contextual environment)

X+B

end

end

- **E** = {A → a, B → b, C → c, AddB → a' }
- **E_C** = $E_{\{B\}}$ = {B → b}